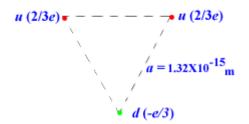
Problem 30.1 (RHK)

In the quark model of fundamental particles, a proton is composed of three quarks: two "up" quarks, each having charge +2e/3, and one "down" quark, having charge -e/3. Suppose that the three quarks are equidistant from each other. We can take the distance this distance to be 1.32×10^{-15} m. We will calculate (a) the potential energy of the interaction between the two "up" quarks and (b) the total potential energy of the system.



Solution:

(a)

Distance between the two "up" quarks, a, is 1.32×10^{-15} m.

Charge of each "up" quark, q, is +2e/3.

Therefore, the potential energy of the two "up" quarks will be

$$U(u,u) = \frac{1}{4\pi\varepsilon_0} \times \frac{(2e/3)^2}{a} = \frac{8.99 \times 10^9 \times 4 \times (1.6 \times 10^{-19})^2}{9 \times 1.32 \times 10^{-15}} \text{ J}$$
$$= 7.749 \times 10^{-14} \text{ J}$$
$$= 484 \text{ keV}.$$

(b)

The total electric potential energy of the 2 "up" and 1 "d" quark system will be

$$U(u,u,d) = \frac{1}{4\pi\varepsilon_0} \left(\frac{4}{9}e^2 - \frac{2}{9}e^2 - \frac{2}{9}e^2 \right) = 0.$$